



CHAPTER - 2  
POLYNOMIALS

**1) Algebraic Expressions:** Any expression containing constants, variables, and the operations like addition, subtraction, etc. is called as an algebraic expression.

**For example:**  $5x$ ,  $2x - 3$ ,  $x^2 + 1$ , etc. are some algebraic expressions.

**2) Polynomials:** The expression which contains one or more terms whose variables have non-negative integral powers is called a polynomial. A polynomial can have any number of terms.

**For example:**  $10$ ,  $a + b$ ,  $7x + y + 5$ ,  $w + x + y + z$ , etc. are some polynomials.

**(3) Polynomials in One Variable:** The expression which contains only one type of variable in entire expression is called a polynomial in one variable.

**For example:**  $2x$ ,  $a^2 + 2a + 5$ , etc. are polynomials in one variable

**4) Term:** A term is either a single number or variable and it can be combination of numbers and variable. They are usually separated by different operators like +, -, etc.

**For example:** Consider an expression  $6x - 7$ . Then, the terms in this expression are  $6x$  and  $-7$ .

**(5) Coefficient:** The number multiplied to variable is called as coefficient.

**For example:** The coefficient of the term  $2x$  will be 2.

**(6) Constant Polynomials:** An expression consisting of only numbers not variables is called as constant polynomial.

**For Example:**  $7, -27, 3$ , etc. are some constant polynomials.

**(7) Zero Polynomial:** The constant polynomial 0 is called as zero polynomial.

**(8) Polynomials in One Variable:**

Let us take an example to understand it:

If the variable in a polynomial is  $x$ , then we can denote the polynomial by  $p(x)$  or  $q(x)$  etc.

*For example:  $p(x) = 7x^2 + 7x + 7$ ,  $t(r) = r^3 + 2r + 1$ , etc.*

**(9) Monomials:** The expressions which have only one term are called as monomials.

*For Example:  $p(x) = 3x$ ,  $q(a) = 2a^2$ , etc. are some monomials.*

**(10) Binomials:** The expressions which have two terms are called as binomials.

*For example:  $r(x) = x + 10$ ,  $c(z) = 7z^2 + z$  etc. are some binomials*

**(11) Trinomials:** The expressions which have three terms are called as trinomials.

*For example:*  $p(x) = 7x^2 + x + 7$ ,  $d(t) = t^3 - 3t + 4$ , etc. are some trinomials.

**(12) Degree of polynomial:** The highest power of the variable in a polynomial is called as the degree of the polynomial.

*For Example:* The degree of  $p(x) = x^5 - x^3 + 7$  is 5.

**Note:** The degree of a non-zero constant polynomial is zero.

**(13) Linear polynomial:** A polynomial of degree one is called a linear polynomial.

*For Example:*  $2x - 7$ ,  $s + 5$ , etc. are some linear polynomials.

**(14) Quadratic polynomial:** A polynomial having degree two is called a quadratic polynomial. In general, a quadratic polynomial can be expressed in the form  $ax^2 + bx + c$ , where  $a \neq 0$  and  $a, b, c$  are constants.

**For Example:**  $x^2 - 9$ ,  $a^2 + 7$ , etc. are some quadratic polynomials.

**(15) Cubic polynomial:** A polynomial having degree three is called a cubic polynomial. In general, a cubic polynomial can be expressed in the form  $ax^3 + bx^2 + cx + d$ , where  $a \neq 0$  and  $a, b, c, d$  are constants.

**For Example:**  $x^3 - 9x + 2$ ,  $a^3 + a^2 + a + 7$ , etc. are some cubic polynomials.

**(16) General expression of polynomial: A polynomial in one variable  $x$  of degree  $n$  can be expressed as:**

$$a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0$$

**where  $a_n \neq 0$  and  $a_0, a_1, \dots, a_n$  are constants.**

**(17) Points to remember :**

- (i) A non-zero constant polynomial has no zero.**
- (ii) A linear polynomial has one and only one zero.**
- (iii) A zero of a polynomial might not be 0 or 0 might be a zero of a polynomial.**
- (iv) A polynomial can have more than one zero.**